

# **Co-Optimization of Fuels & Engines**

#### FOR TOMORROW'S ENERGY-EFFICIENT VEHICLES

**Co-Optima Simulation Toolkit Team** 

June 9, 2016



FT040

# **Co-Optimization of Fuels and Engines** (Co-Optima) – Simulation Toolkit Team

# June 9<sup>th</sup>, 2016

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- 1. Lawrence Livermore National Laboratory
- 2. Argonne National Laboratory
- 3. Los Alamos National Laboratory
- 4. Oak Ridge National Laboratory
- 5. National Renewable Energy Laboratory
- 6. Sandia National Laboratories

# Co-Optima DOE Management Team:

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- 1. Project Overview
- 2. Relevance
- 3. Team Approach
- 4. Task Approach and Relevance
- 5. Tracked Milestones
- 6. Reviewer Comments



## **Overview**

# Timeline

Project start date:FY16Project end date:FY19\*Percent complete:20%

# **Barriers and Challenges**

**<u>Complexity</u>:** Accurately modeling new fuels and their impact on engine performance requires analysis tools and expertise spanning more than a dozen software packages and several research groups.

**<u>Timing</u>**: Schedule for completing R&D and achieving market impact is extremely ambitious.

#### Budget

- Funding for FY16: \$2.1M
  - VTO funding: \$2.1M

**\$0** 

BETO funding:

#### **Partners**

#### **External Advisory Board:**

- USCAR
- Advanced Biofuels Association
- EPA
- Dave Foster (U. Wisc)
- Truck & Engine Manufacturers Association

#### Stakeholders:

- API
  - Fuels Institute
- CARB
- UL
  - Joe Norbert (U.C. Riverside)
- 85 individuals representing 46 organizations

\* End date for Thrust I (spark ignition R&D); Thrust II (advanced compression ignition) R&D will continue



Core tasks for the 18- month decision point:

1. Develop and test the Co-Optima Central Fuel Hypothesis



- Extend the fuel & engine parameter space for conditions that can not be tested due to cost, time, or physical constraints
- Test new fuel property combinations virtually using simulations
- 2. Identify and refine the coefficients in the Co-Optima Merit Function (a.k.a., the Miles Merit Function) that capture the impact on of fuel properties on engine performance
  - Compute sensitivity of coefficients with validated simulations using high-throughput HPC resources
- 3. Establish the constraints for the scenario analysis "optimizer"
  - Create the software to find optimized scenarios from the Co-Optima generated data and constraints



# Approach: Assemble a highly skilled team of DOE VTO researchers



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# Approach: Leverage existing VTO software and expertise spanning the simulation space





# Approach: Build a shared community around computing and data to accelerate research

#### **Shared Computing Resources:**

- Peregrine at NREL
- 58K Intel Xeon CPUs
- 60M cpu-hour Co-Optima allocation for FY16
- Access for all Simulation Toolkit team members

Shared Data & Tools:









# Task G.1. Fuel Property Simulations

- Task G.1.1 Blending model for simulation inputs
- Task G.1.2 Simulation support for small volume fuel testers
- Task G.1.3 Simulation support for kinetic mechanism development and canonical fuel experiments



# Task G.2. Advanced Engine Simulations

Task G.2.1 – Extreme mechanism reduction for advanced spark ignition engines (DISI)

# Task G.3. Blendstock-to-Efficiency (B2E) Application

Create and validate a comprehensive workflow to simulate the impact of a new fuel composition on engine performance





#### • Goal:

Model any new and existing fuel blendstocks considered by Co-Optima in the suite of VTO software tools for combustion and engine analysis

#### • Approach:

Create, test and validate thermophysical and chemical kinetic input estimation and generation techniques.



- Temperature
- Viscosity
- Surface Tension
- Enthalpy of Vapor.
- Vapor Pressure
- Thermal Conductivity
- Density
- Specific Heat



Adjust surrogate composition or key reaction rates to capture:

- AKI
- Sensitivity
- Distillation Curve
- H/C Ratio, PIONA
- RCM data
- IQT data
- $\mu$ FIT data
- virtual CFR



#### • New capabilities and analyses:

- Virtual tests to map changes in thermodynamic, transport, kinetic parameters to properties that characterize fuel performance or quality
- Creation of virtual fuels with optimized properties
- Simulation of Thrust I kinetic blending behavior experiments (e.g. IQT)
- Use simulations to answer "what property range does an engines want?"

#### • Co-Optima Impact:

 Creates the necessary tools to test and validate the Central Fuel Property hypothesis and the Co-Optima Merit Function sensitivity coefficients



#### • Goal:

Reach the "game-changing" volume and throughput identified by B. Simmons (Co-Optima All Hands Mtg., Feb. 2016)

- 20  $\mu$ L samples at 100s of tests/mo
- Approach:
  - Develop new techniques to extract or infer kinetic data from experiments via sim
  - Simulate design improvements to increase sensitivity, reduce sample volume and increase throughput
- Co-Optima Impact:
  - Dramatically lower the barrier to new fuel blendstock discovery
  - Create a rich set validation data for training new fuel chemistry models



#### μL Fuel Ignition Tester





#### • Goal:

Accelerate the development and use of new, detailed kinetic mechanisms for the Co-Optima program

- Approach:
  - Create any new or missing reaction classes to capture non-linear fuel blending interactions
  - Create new analysis tools using Zero-RK to more rapidly evaluate, validate or infer fuel kinetic information from canonical Co-Optima experiments (e.g., shock tubes, rapid compression machines, or flow reactors)

#### • Co-Optima Impact:

- Delivers more accurate fuel chemistry in a shorter time to the Co-Optima

analysis

Rapid Compression Machine (RCM) Goldsborough/ANL







- Improve time to result of the simulations
- Improve accuracy of predictions
- Approach: Uncertainty Quantification (UQ)

Derive extremely reduced chemical mechanisms using Bayesian inference

- Decrease CPU cost while capturing kineticdependent quantities of interest (ignition delay time, flame speed, heat release, *etc*.)
- Produce quantified error bars
- Co-Optima Impact:
  - Quickly define chemical mechanisms based on new experimental measurements of biofuels (detailed mechanisms not needed)
  - Improve predictions and turn-around time of the Toolkit Team simulations 100x faster







- Goal:
  - Create and validate a comprehensive and efficient workflow to simulate the impact of a new fuel composition on engine performance
- Approach:
  - Leverage simulation input generation from G.1.1
  - Conduct detailed single cylinder CFD calculations (ConvergeCFD & Kiva-hpFE) for advanced SI experiments to produce ethanol blending trends
  - Use single cylinder blending trends in multi-cylinder (GT-Power) analysis of multi-cylinder Thrust I experiments
  - Link multi-cylinder analysis to Autonomie model (funded by VSS185) for vehicle system efficiency
- Co-Optima Impact:
  - Create a common language and workflow for faster analysis
  - Validate Co-Optima simulation tools





**PIV- Experiment** 



CFD - Simualtion

- Measure and fix workflow bottlenecks
- ID greatest sources of uncertainty



Due	Туре	Milestones	Status
9/30/2016	reg.	Provide a report to DOE and Co-Optima team on the performance of the simulation parameter generation techniques (owner NREL)	on schedule
9/30/2016	reg.	Provide a report to DOE and Co-Optima team on the current development status and potential for each of the three small volume fuel testing techniques (owner LLNL)	on schedule
9/30/2016	reg.	Provide a report to DOE and Co-Optima team on the ability to simulate the chemical kinetics and RCM for the new and existing fuels considered in FY16 (owner LLNL)	on schedule
9/30/2016	reg.	Provide a report to DOE and Co-Optima team on the performance of the extreme mechanism reduction for modeling advanced SI engines (owner SNL)	on schedule
9/30/2016	reg.	Provide a report to DOE and Co-Optima team on the ability to simulate the blendstock's engine impact for the Thrust 1 experiments using existing simulation capabilities for new and existing fuels (owner ANL)	on schedule



Almost all of the Simulation Toolkit team's FY16 research is a new start. The following are responses to some of last year's VTO projects that are relevant to the Co-Optima program's goals.

1. [ACE012] "there are a number of programs all funded in ACE which could be better integrated including, KIVA, high fidelity LES, computational speedup, to make sure that the technologies developed by DOE work together and feed into needed improvements"

The Simulation Toolkit team was designed from the start to go beyond the traditional organization of our research programs. All of our tasks require close collaboration across laboratories, simulation capabilities, and the other Co-Optima teams. To be successful, we have created a community of shared computing and tracked data repositories hosted by NREL. The team represents all the ACE simulation efforts and has made significant joint progress in the first six months of Co-Optima. Further, Task G.3 (Blendstock-to-Efficiency Application) is designed to integrate all the VTO and (eventual) University partners in a common framework. This will provide the Co-Optima program the following: tremendous time savings in human and CPU costs; more rigorous comparison of approaches; and 2. [ACE075] "The portfolio of work should be adjusted so more gasoline sprays and combustion are being modeled if one hopes to impact petroleum consumption of the LD fleet."

The Simulation Toolkit team selected the Advanced SI engine experiments with gasoline and bio-derived blendstocks for Task G.3 (Blendstock-to-Efficiency Application). This case was deliberately chosen to expand and validate our simulations using a challenging, but very relevant near-term application. Our research plan reflects a large increase in the VTO portfolio to include gasoline spray combustion modeling.

3. [FT026] "Micro-FIT is an important breakthrough to experimental fuel volumes/cost."

The Co-Optima program recognizes the enormous potential to accelerate new fuels research by developing small volume, high throughput kinetic measurements. Simulation is essential to increase the sensitivity and accuracy of new devices like micro-FIT and to extract kinetic data from the IQT and RCM. Simulation Toolkit tasks G.1.2 and G.1.3 directly supports these efforts.



**Fuel** 

Engine

I owGHG

**Fuel** 

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Surrogate Optimizer

Created an automated fuel surrogate optimizer to produce more realistic chemistry models for new blendstocks





#### Surrogate Optimizer

The surrogate optimizer offers a large time savings over the "handtuned" approach previously used by the Fuel Properties team.

- Efficiently computes large mechanisms (+2000 species)
- Each calculation 10-15x faster than commercial solvers
- Available now on peregrine for all Co-Optima teams
- Targets captured more accurately than hand-tuned methods



## **Future Work:**

- Add RCM experimental data
- Add distribution of carbon bond types
- Update AKI/Sensitivity correlations with virtual RON & MON tests



## Accomplishment: Task G.1.1 - Blending Model for Simulation

#### Sensitivity of ignition delay time to fuel composition

- OD ignition delay (with Cantera) calculations
   performed for different
   PRFs and E30 compositions
- Sensitivity of ignition delay time to composition for PRF and E30 blends
- This forms part of the overall relation between performance and blend composition
- For E30 changes in isooctane fraction have much more impact
  - Could impact dominant term







Accomplishment: Task G.1.1 - Blending Model for Simulation

Identification of flow reactor targets to improve accuracy

- Sensitivity study to changing PRF composition (ΔΟΝ)
  - Detailed mechanism (LLNL supplied)
  - 1 atm, 700-900k, constant P reactor
  - Variety of times up to 0.1ms
  - Species sorted by sensitivity to ON based on PRF composition
- Highest sensitivity at lower temperatures for same time (earlier in ignition process)



Needs to be repeated with more complicated fuels, in conjunction with virtual CFR models to map kinetics/composition to properties



## Accomplishment: Task G.1.1 - Blending Model for Simulation

#### Blending model for biofuel thermophysical properties

*Detailed treatment of thermodynamics and transport properties for multicomponent fuels:* 

- Real-fluid mixture properties obtained using Extended Corresponding States model
- Multicomponent formulation using cubic (PR/SRK) or BWR equations of state
- Generalized to treat wide range of biofuel blendstocks (Fuel/Oxidizer/Products)

#### <u>Provides Tabulated Input for</u> <u>Project Codes (e.g., CONVERGE):</u>

- Temperature
- Viscosity
- Surface Tension
- Enthalpy of Vaporization
- Vapor Pressure
- Thermal Conductivity
- Density
- Specific Heat

e.g., Variation in liquid-gas density and viscosity for E30 as function of pressure and temperature shown on right





Thermal model for µFIT improves measurement accuracy

Created a detailed thermal model to quantify the temperature difference between the thermocouple and the wall conditions

The micro-liter Fuel Ignition Tester (µFIT) uses an unsteady flame in a mm-scale channel to measure fuel chemistry



μFIT prototype operating at LSU by Schoegl under the Co-Optima Fuel Properties team (propane shown)



Detailed modeling uncovered:

- thermocouple holder affects the measured temperature in the tube
- thermocouple translation speed originally too fast
- +30K measurement error corrected in less than a week



#### Use simulations to extend µFIT applicability

Accurate wall temperature measurements are critical to enable the extraction of kinetic information  $\mu$ FIT from using simulation

Wall temperature measurement in action





#### Future Work:

- quantify the model sensitivity and uncertainty resolving the wall temperature profile
- redesign (with LSU) the external heating profile to increase the measurement sensitivity for low temperature heat release
- determine the flow and heating conditions needed to operate μFIT at pressures greater than 30 bar



#### Accomplishment: Task G.1.2 - Small Volume Fuel Testers

#### Virtual CFR Engine\* based on CFD to estimate RON and MON

- Bore = 8.265 cm, stroke = 11.43 cm, connecting rod = 25.4 cm, swept volume = 613.25 cc, CR = 7
- $T_{IVC} = 54.5^{\circ}$  C,  $P_{IVC} = 1.145$  bar, cylinder jacket temperature =  $81^{\circ}$  C, engine speed = 900 RPM
- 3D Closed cycle RANS motoring simulations from IVC to EVO are performed and shown to match well with experiments

#### **Future Work**

- Full cycle RANS and LES of CFR engine incorporating gas exchange processes, at fired conditions
- Knock capturing with CONVERGE using adaptive mesh refinement
- Virtual RON/MON simulation tests for gasolineethanol blends, validation against experimental data from CFR engines and development of novel theoretical correlations to rapidly determine octane numbers
- New CFR engine at ANL to provide experimental data in future
- \* Current CFR engine surface mesh provided by Dr. Ben Wolk (SNL) and Prof. J.Y. Chen (UCB)
- \* CFR engine data provided by Dr. Vi Rapp at LBNL





Ignition Quality Tester experiments and simulations

<u>Objective</u> is to study **ability of surrogate mechanism to capture sensitivity to surrogate fuel compositions** in a multi-physics environment

- Prof. G. Bogin (CSM) will conduct CONVERGE simulations of IQT experiments for ethanol & iso-octane blends
- Iso-octane baseline established, binary and reference blends being simulated now
- Online mechanism reduction (DRG) included to establish appropriate level of reduction in mechanism for capturing realistic ignition process

Future Work:

 Capturing sensitivities to kinetics dependent properties requires simulations that can propagate kinetics sensitivity through CFD calculation, including turbulence-flame interaction





Created two new Zero-RK tools to analyze experiments

Developed new tools for high throughput modeling of the constant pressure flow reactor experiments (NREL) & RCM experiments (ANL)



- Simple Zero-RK interface created on peregrine to couple with existing NREL python tools
- +200x speedup over Cantera for the target Thrust 1 mechanism
- Batch processing of RCM simulations has high throughput for automated optimization of new fuel surrogates
- New Zero-RK tool avoids large human setup cost (and errors)



#### Create Zero-RK multizone models of experiments

Increase the accuracy of the high-throughput, chemical kinetics tools to test the Co-Optima central fuel hypothesis, and rapidly evaluate the sensitivity of the merit function coefficients.



- Develop a multizone model for virtual RON and MON experiments
- Test virtual RON and MON models in the surrogate optimization loop



 Accelerate the RCM model of Goldsborough (CNF 2012) to capture crevice effects with Zero-RK Accomplishment: Task G.1.3 - Kinetic Mechanism Development

#### **Thrust 1 mechanism reduction**



- ✓ Pressure: 1-100 atm
- ✓ Equivalence ratio: 0.5-2.0
- ✓ Initial temperature: 700 1800 K

- Surrogate mixture identified through the surrogate blend optimizer developed under Co-optima (for different blends of gasoline with alcohols)
- Detailed mechanism developed at LLNL and validated against RCM data at ANL
- Mechanism reduction performed in collaboration with Prof. Tianfeng Lu at University of Connecticut (was being done under NSF-DOE collaboration between UConn and ANL)
- Expected accuracy of the reduced mechanism is shown below. This reduction was performed for ndodecane molecule





**Objective:** Capture auto-ignition delay time for any molecule at engine conditions



Form of the optimized mechanism for  $n-C_{12}H_{26}/Air$ :

 $\ln A = \lambda_0$ 

$$C_{12}H_{26} + 12.5O_{2} \rightarrow 12CO + 13H_{2}O$$

$$CO + 0.5O_{2} = CO_{2}$$

$$k_{1} = A \exp(-E_{a} RT)[C_{12}H_{26}]^{0.25}[O_{2}]^{1.5}$$

$$k_{2} = 3.98 \times 10^{14} \exp(-40/RT)[CO]^{1}[H_{2}O]^{0.5}[O_{2}]^{0.25}$$

$$k_{-2} = 5.00 \times 10^{8} \exp(-40/RT)[CO_{2}]^{1}$$
Coefficient from Westbrook CST 1981

The parameter **A** is actually a complex function (found by least-square fitting) of  $T_0$  and  $\phi$  to capture non-linear behavior of ignition delay:  $E_a = \eta_0$ Those are the parameters to infer

 $+\lambda_3 \tanh(\lambda_4 + \lambda_5 \phi)T_0 + \lambda_6$ 



#### Accomplishment: Task G.2.1 - Extreme Mechanism Reduction

#### **Optimized reduced mechanisms with <5 species**

• Build surrogate and use Bayes' rule to find parameters (pdf)



• Mechanism performance:



Sampling performed using Metropolis Markov Chain Monte Carlo (MCMC):

- High-dimensional complex (non-Gaussian) using
   Monte Carlo
- Contains adaptation and rejection rules
- 200 000 samples required to get parameters



Future work will focus on Thrust I Ethanolgasoline blends and bio-diesels



#### Accomplishment: Workflow development

- Unify multiple simulation components into a single toolchain
- Analyze candidate fuels from composition and basic properties through whole-vehicle analysis



Accomplishment: Task G.3 - Blendstock-to-Efficiency Application

#### High-fidelity DISI engine geometry creation

Head geometry previously unknown

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- An X-ray scan of the head was combined with known piston, intake and exhaust geometries
  - CAD and X-ray data courtesy of Sjöberg at Sandia
- The X-ray scanned geometry needed to be cleaned and merged with the known CAD geometry
  - Done jointly with Scarcelli at Argonne
- Full geometry now available to all Co-optima groups



#### Sample X-ray feature needing correction



Clean X-ray Head Scan



Open-cycle CFD Geometry



Accomplishment: Task G.3 - Blendstock-to-Efficiency Application

#### **DISI Engine Simulations**

- High-swirl motored engine case
  - One valve deactivated
  - No fuel injection

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- Nominal compression ratio: 12:1
- Typical timing: fuel injection -30° aTDC, spark -25° aTDC
- Intake Pressure: 94 kPa
- Intake Temperature: 31° C
- CFD simulations performed with CONVERGE software
  - Large-eddy Simulations (LES) with Dynamic Structure turbulence model
- Crank-angle resolved pressure and temperature boundaries
- Wall boundary temperatures estimated from measured coolant temperatures
- Need to verify wall boundary temps



- Measured pressures not precisely aligned with CFD domain boundaries, need to account for phase shifting
- Engine compression ratio needs to be verified



- Particle Image Velocimetry (PIV) measurements in swirl and tumble planes from Sandia
- Data from -30° aTDC, near nominal injection timing
- Simulation data from 2<sup>nd</sup> LES cycle (i.e., not ensemble averaged)

**LES Simulation Experiment PIV Cutting Plane Schematic** Velocity (m/s) Swirl Tumble 



- production GM 1.9 L diesel engine run on gasoline compression ignition mode (GCI)
- CFD used to optimize combustion using CONVERGE code
- Global Sensitivity Analysis (GSA) on fuel properties







Accomplishment: Task G.3 - Blendstock-to-Efficiency Application

#### Effect of Fuel properties on engine performance

variable	description	baseline	min	max
T <sub>(f,crit)</sub>	fuel critical temperature	540 k	530 k	550 k
Density	fuel density	1.00	0.95	1.05
HOV	fuel heat of vaporization	1.0	0.9	1.1
VP	fuel vapor pressure	1.0	0.9	1.1
Viscosity	fuel viscosity	1.0	0.7	1.3

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- Fuel properties varied (in Monte Carlo fashion) to demonstrate the capability of GSA tool
  - Fuel property variations (in this range) have a significant influence on CA50
    - Fuel HOV and critical temperature seem to influence CA50



### Future Work: Task G.3 - Blendstock-to-Efficiency Application

#### Effect of Fuel properties on DISI engine performance

#### Sandia DISI Engine

- Validate gas-exchange flow and combustion
- Simulate multiple engine operating conditions
  - Both those measured experimentally and those not
- Perform GSA for fuel property effects similar to the one done for GCI analysis









#### Future Work: Task G.3 - Blendstock-to-Efficiency Application

#### Linking engine simulations to efficiency





Single cylinder engine modeling with KIVA-hpFE

## • Fielding KIVA-hpFE to model engine performance w/new fuels

1. Grid developed for Thrust I DISI engine (Sjoberg, SNL) and other chosen engines (ongoing)



GridPro mesh for Intake Manifold of Sandia DISI engine taken from X-ray generated faceted surface

- 1. Chemkin chemistry solver functionality in KIVA-hpFE (ongoing)
  - collaborating with ANSYS's Reaction Design group
- 2. Incorporate realistic thermophysical properties for liquid fuel blendstocks
- 3. Perform full engine simulation for Thrust I engine and fuels



#### Multi-cylinder engine performance modeling

#### Multi-cylinder simulation studies at Oak Ridge National Laboratory

- Full-engine GT-Suite simulations of 1.6-L Ford GDI engine
- Supports experimental, high-octane fuel studies (Sluder/ORNL)

# Efforts will expand upon experimental capabilities to further explore potential benefits of high-octane fuel blends

- Explore enhanced boosting strategies to enable additional engine down-sizing
- Coupled GT-Power/CONVERGE simulations in collaboration with ANL to explore fuelvaporization and knock onset
- Provide engine maps to ANL for fuel-economy simulations with Autonomie



Hardware scans and engine measurements necessary for constructing the 1-D and CFD geometry models are underway

**1.6-L Ford GDI engine installed in dynamometer cell at ORNL** 







Important to account for uncertainty



# **Summary of FY16 Accomplishments**

#### shared data & resources



# better experimental accuracy

#### real geometry CFD validation



# faster setup time for new fuels







# Approach/Strategy: Six Integrated Teams



Identify promising bioderived blendstocks, develop selection criteria for fuel molecules, and identify viable production pathways





Identify critical properties and allowable ranges, systematically catalogue properties, and predict fuel blending behavior





Quantify interactions between fuel properties and engine design and operating strategies – enable optimal design of efficient, emission-compliant engines



Extend the range, confidence and applicability of engine experiments by leveraging high-fidelity simulation capabilities



Analyze energy, economic, and environmental benefits at US economy-level and examine routes to feedstock production at scale through existing biomass markets Identify and mitigate challenges of moving new fuels and engines to markets and engage with full range of stakeholders



- 1. Get **experimental data on new fuels** from other Co-Optima teams (i.e. ignition delay time) over ranges of interest (P, T, phi)
- 2. Define the **"form" of the optimized chemical mechanism** (2, 4, 6 steps, and the uncertain chemical parameters). The approach helps finding the unknown chemical parameters
- 3. Build **surrogate (Polynomial Chaos Expansion)** of the chemical model: homogenous reactor simulations used to find the surface response of the mechanism in parameter space.
- 4. Use **Bayes' Rule and PCE to find chemical parameters** of optimized mechanism
- 5. Propagate parameters' uncertainties to get error bars on prediction

Bayes formula gives the joint PDFs on parameters of interest (called posterior):

Fvidence



- Prior: knowledge on the parameters (ranges, ...)
- Likelihood: obtained by sampling the PCE in parameter space
- Evidence: normalizing constant in the present context