



# Mg<sub>2</sub>Si Composites with Embedded Si Nanoparticles for Energy Recovery of Waste Exhaust Heat

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Industrial partners: **NASA JPL; BSST LLC**

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# Overview

## Timeline

Start: September 2010

End: August 2013

15% complete

## Budget (DOE funding)

**2010-11**

**UCSC \$71K; UC Davis \$71K**

**2011-12**

**UCSC \$75K; UC Davis \$75K**

## Partners

- UCSC (Shakouri, Bian) –lead (transport modeling and thermoelectric characterization)
- UC Davis (Kauzlarich) (material synthesis, structural characterization)
- In collaboration with JPL (Fleurial) and BSST (Bell) (verify thermoelectric measurements, study material uniformity, advice on scale up production)

## Barriers

- **Cost** (improve ZT of abundant/non-toxic TE materials)
- **Scale up to practical TE device** (use of bulk synthesis techniques)



## Project Objective:

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□ To develop environmentally benign, nanostructured materials that are grown in bulk for enhanced thermoelectric performance ( $ZT > 1.3-1.8$ ) in 500-800K range for direct conversion of waste exhaust heat into electricity.



# Milestones:

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## ▶ Year 1

- ▶ Synthesis and characterization of n-type  $\text{Mg}_2\text{Si}$  and  $\text{Mg}_2\text{Si}_x\text{Sn}_{1-x}$  with embedded nanoparticles
- ▶ Boltzmann transport modeling of electron mobility and Seebeck coefficient for  $\text{Mg}_2\text{Si}$  alloys (include nanoparticle scattering)
- ▶ Thermal conductivity modeling including nanoparticle scattering

## ▶ Year 2

- ▶ Synthesis and characterization of p- $\text{Mg}_2\text{Si}$  alloys with nanoparticles
- ▶ Boltzmann transport modeling of hole transport including nanoparticles

## ▶ Year 3

- ▶ Demonstrate n- and p-type  $\text{Mg}_2\text{Si}$  alloys with  $\text{ZT} > 1.8$  and  $> 1.0 - 1.3$  respectively
  - ▶ Full thermoelectric property characterization in 300-800K range; verification at **JPL** and at **BSST**
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## Approach:

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- ❑ Optimize Zintl phase  $\text{Mg}_2\text{Si}$  alloys with embedded nanoparticles (NP) for maximum ZT in temperature ranges for conversion of waste exhaust heat.
- ❑ Optimize NP size and composition to scattering mid/long wavelength phonons and reduce lattice thermal conductivity
- ❑ Optimize NP potential profile to benefit from hot electron (hole) filtering and increase the thermoelectric power factor
- ❑ Use scalable bulk growth techniques

Order	Element	Abundance ratio (%)
2 <sup>nd</sup>	Si	25.8
8 <sup>th</sup>	Mg	1.93



# Progress: Electron Transport Modeling

## Boltzmann Transport

$$\sigma = \int \sigma(E) dE$$

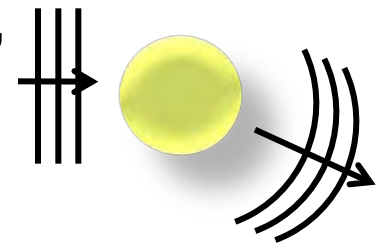
$$S = \frac{1}{eT} \frac{\int \sigma(E)(E - E_F) dE}{\int \sigma(E) dE} \propto \langle E - E_F \rangle$$

## Differential Conductivity

$$\sigma(E) = e^2 \tau(E) v_x^2(E) \rho(E) \left( -\frac{\partial f_0(E)}{\partial E} \right)$$

$$\frac{1}{\tau(E)} = \frac{1}{\tau_{imp}(E)} + \frac{1}{\tau_{phonon}(E)} + \frac{1}{\tau_{nano}(E)}$$

Partial wave method for single particle scattering, exact solution of the Schrödinger equation



**Table 1**

Experimental (300 K) and calculated electronic properties of Mg<sub>2</sub>Si.

Property	Calc. (from literature)	Calc. (this work)	Exp.
Direct gap $\Gamma_v \rightarrow \Gamma_c$ (eV)	1.55 <sup>a</sup> [10], 1.65 <sup>b</sup> [9], 2.20 <sup>c</sup> [10]	1.75	2.27 [7]
Indirect gap $\Gamma_v \rightarrow X_c$ (eV)	1.3 <sup>d</sup> [8], 0.12 <sup>a</sup> [10], 0.65 <sup>c</sup> [10]	0.21	0.66–0.78 [4–6]
Effective mass $m_{\parallel}/m_0$	0.69 [8]	0.58	–
Effective mass $m_{\perp}/m_0$	0.25 [8]	0.19	–

Use band parameters from: Computational Materials Science 50 (2011) 847–851

Developed Boltzmann transport model for Mg<sub>2</sub>Si taking into account two conduction bands and the impurity and phonon scatterings. Nanoparticle scattering was also added using Partial Wave Method.

# Technical Accomplishments

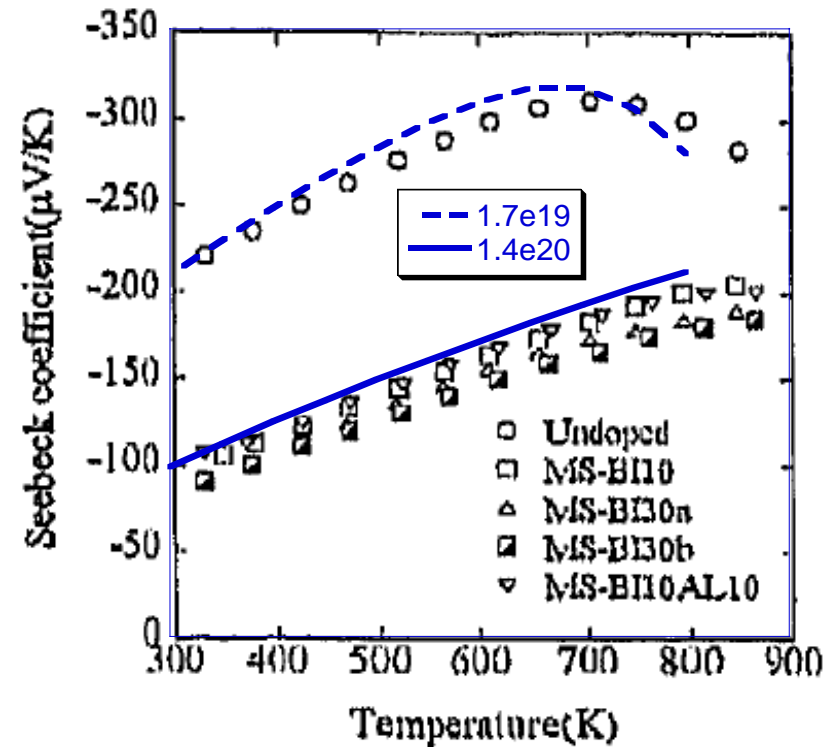
## Electron Transport Modeling

### Modeling of bulk $\text{Mg}_2\text{Si}$ Seebeck

Table I. Grown samples with the results of Hall measurements

Sample name	Bi doping (atom%)	Al doping (atom%)	Carrier concentration $N_D - N_A$ ( $\text{cm}^{-3}$ )	Hall mobility ( $\text{cm}^2/\text{Vs}$ )
Undoped	0.0	0.0	$1.69 \times 10^{19}$	157.9
MS-Bi10	1.0	0.0	$1.38 \times 10^{20}$	95.4
MS-Bi10Al10	1.0	1.0	$1.41 \times 10^{20}$	91.3
MS-Bi30a	3.0	0.0	$1.31 \times 10^{20}$	86.8
MS-Bi30b	3.0	0.0	$1.39 \times 10^{20}$	87.7

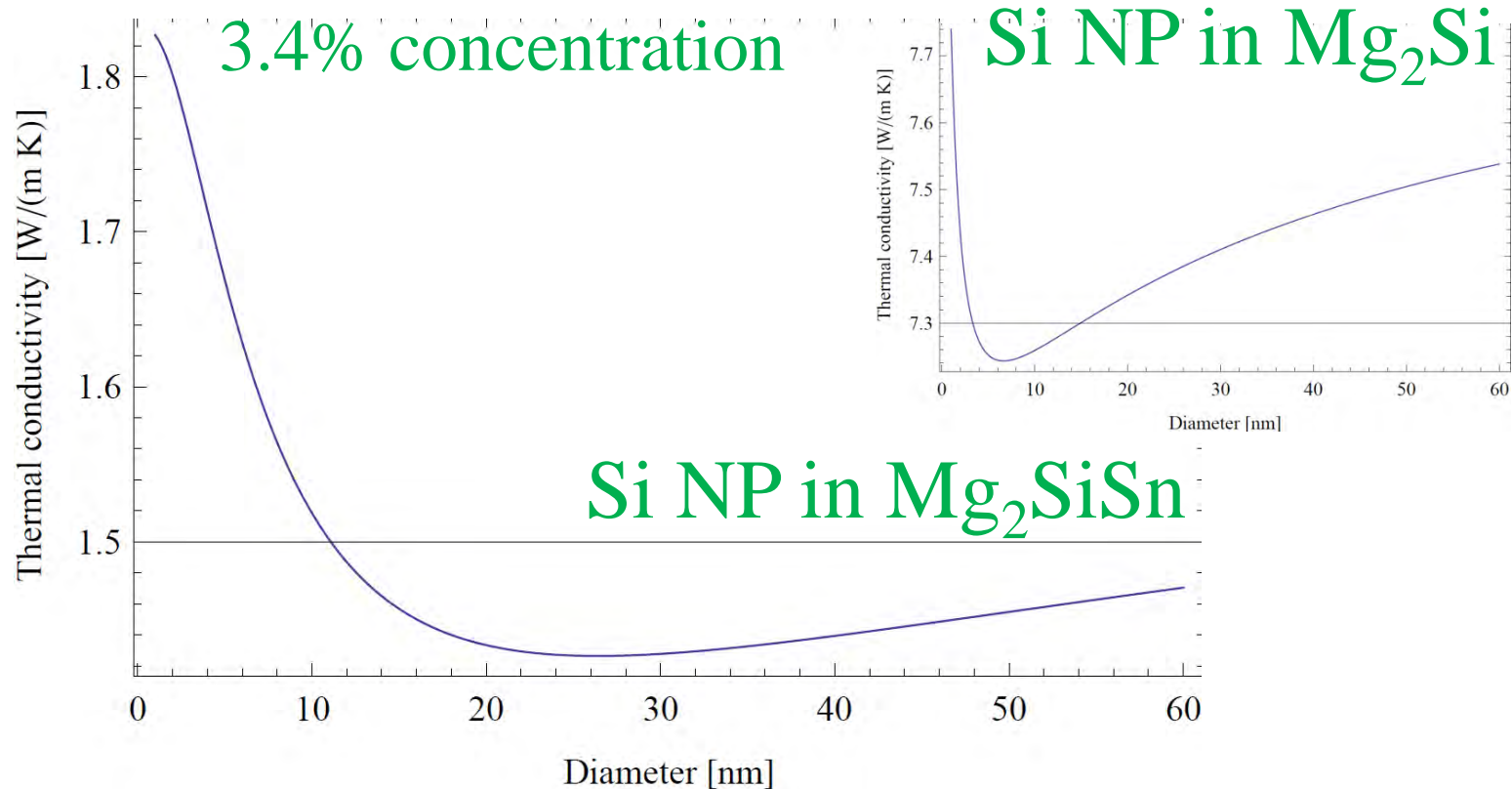
Using experimental data from:  
“Crystal growth of  $\text{Mg}_2\text{Si}$  by the vertical Bridgman method and the doping effect of Bi and Al on thermoelectric characteristics,” MRS fall meeting, 2007



□ Theory can explain both doping and temperature-dependence of the Seebeck Coefficient for n-doped bulk  $\text{Mg}_2\text{Si}$

# Technical Accomplishments

## Phonon Transport Modeling

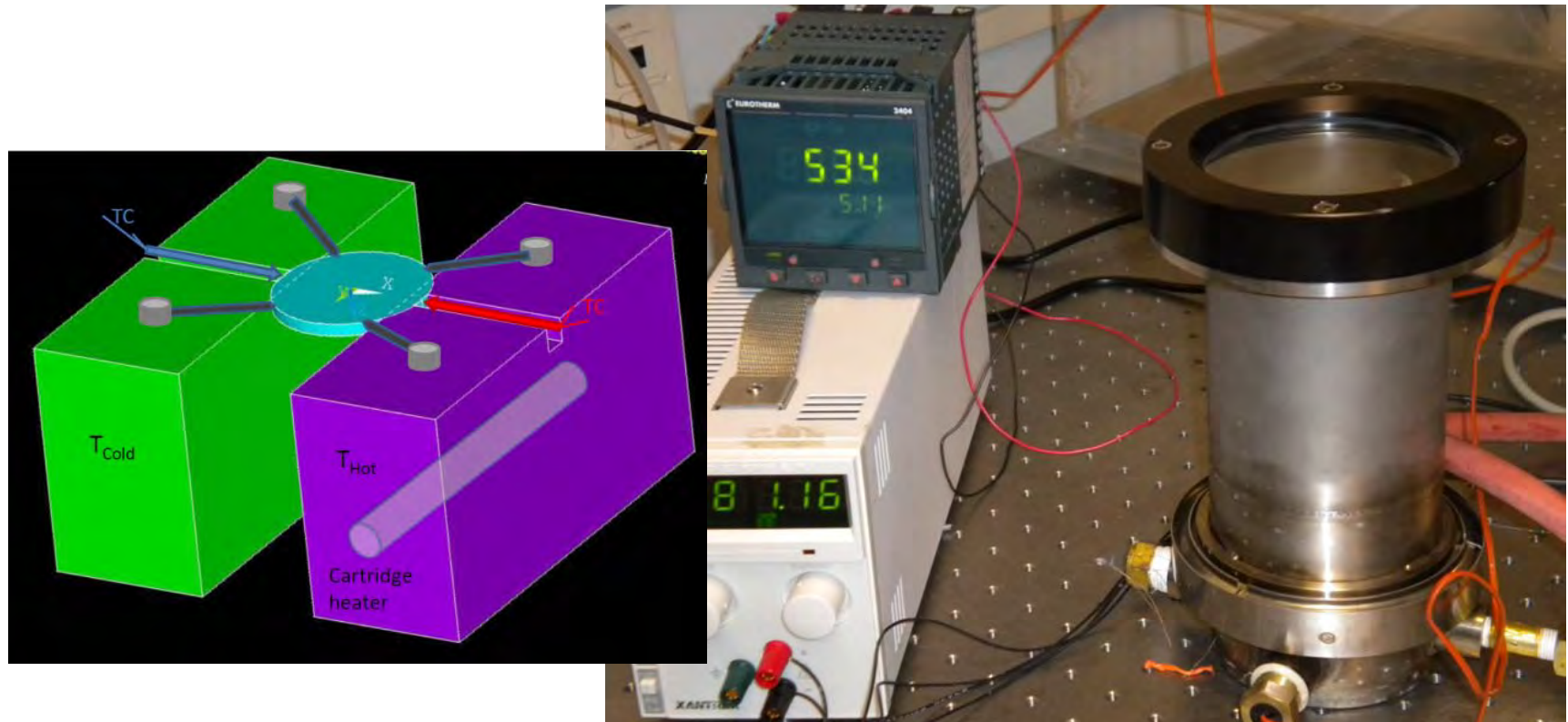


- ❑ Modeled the effect of Silicon nanoparticles on the thermal conductivity of  $\text{Mg}_2\text{Si}$  and  $\text{Mg}_2\text{SiSn}$
- ❑ Optimum nanoparticle size for lowest thermal conductivity identified

# Progress:

## High Temperature Characterization Apparatus

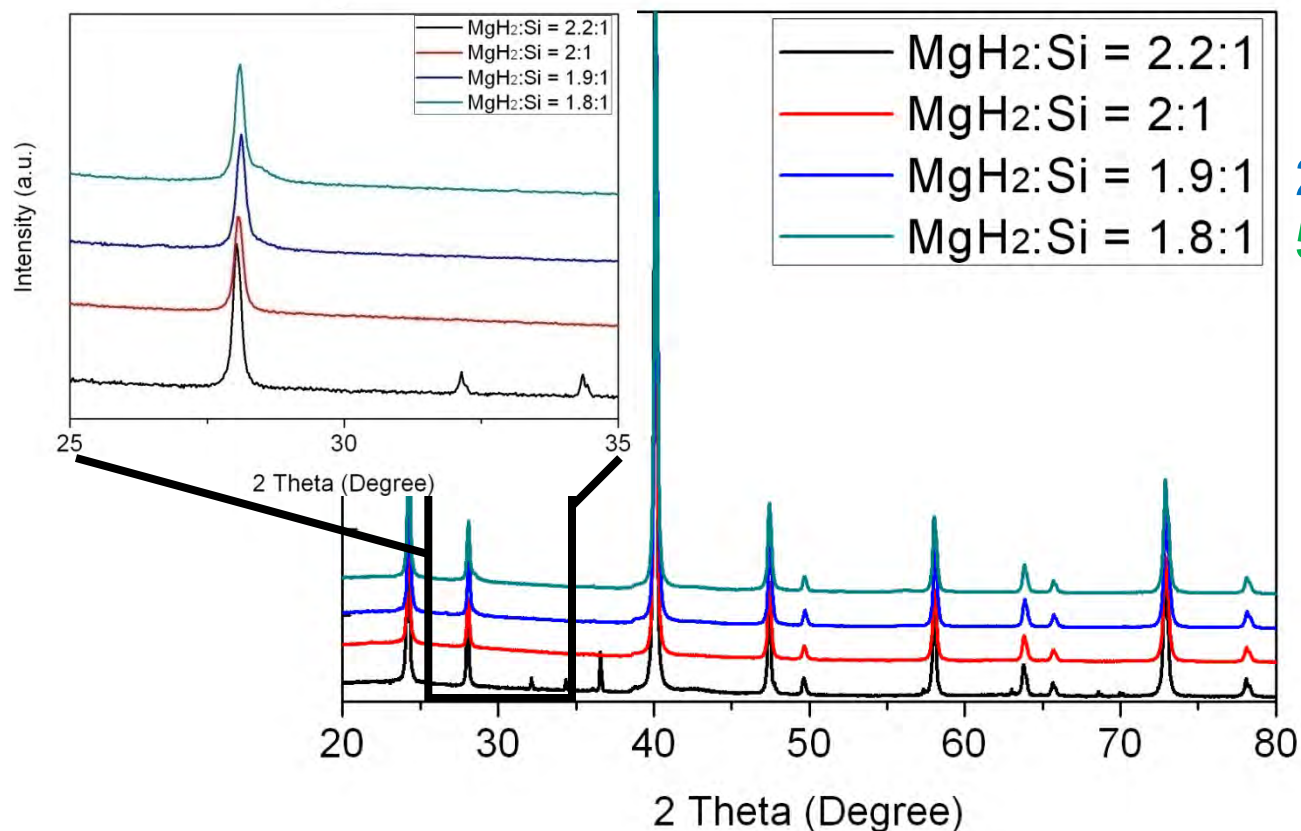
Designed a set up for simultaneous Van der Pauw and Differential Seebeck measurement (in order to characterize the new materials rapidly).



# Progress: Preliminary Material Synthesis



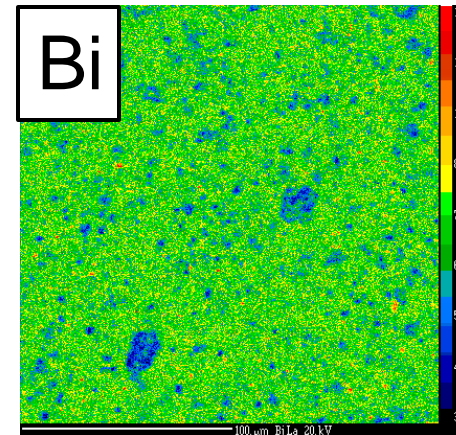
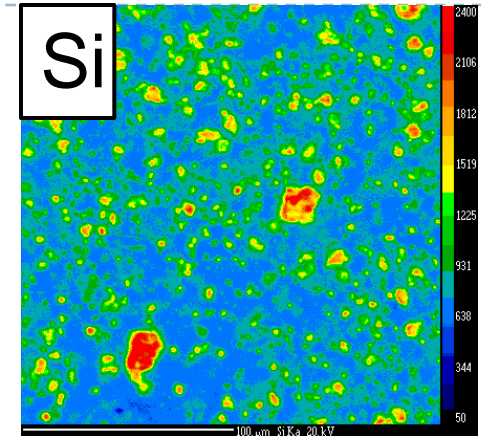
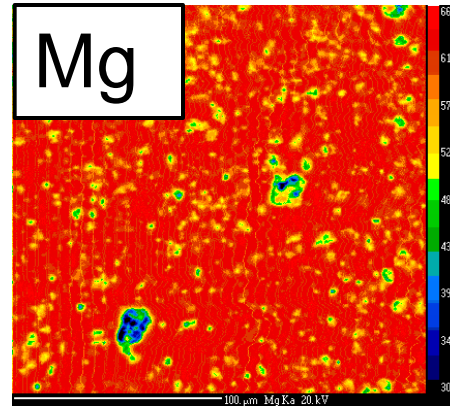
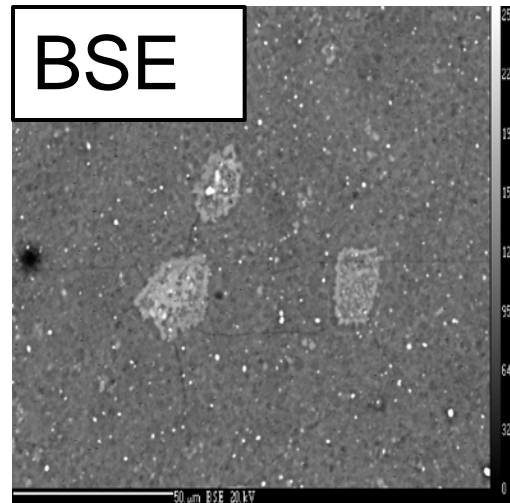
## Powder X-ray Diffraction



Control the amount of nano-Si inclusions through stoichiometry. The very small shoulder on the right of the peak at ~27 degrees is due to Si and we can fit the spectrum to determine the weight percentage and thereby the atomic percentage.

# Progress: Microprobe analysis of $\text{Mg}_2\text{Si}$ with Si Nanoparticles

5% Si, 1% Bi

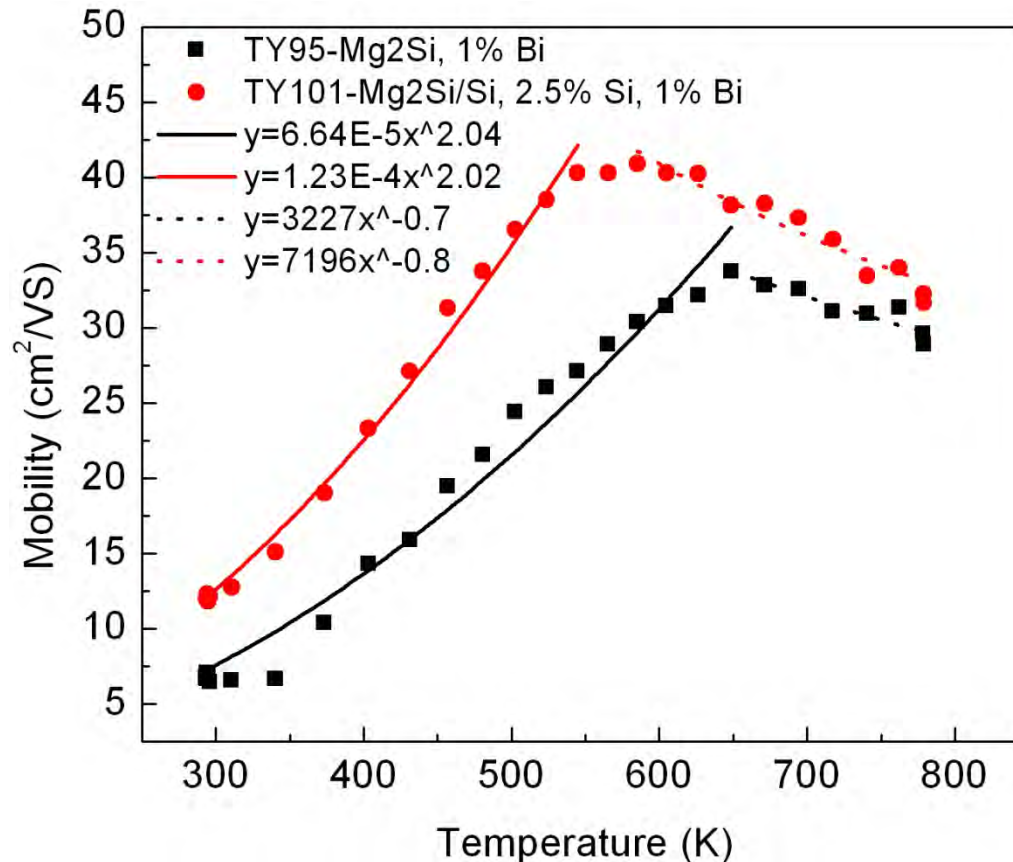


Majority phase  $\text{Mg}_{2.10(2)}\text{Si}_{0.99(3)}\text{Bi}_{0.01(002)}$

Si rich areas are the Bi deficient areas. Therefore, most of the Bi diffused into  $\text{Mg}_2\text{Si}$  matrix. Si rich areas are at micro level, which indicates that Si particles agglomerated.

# Progress

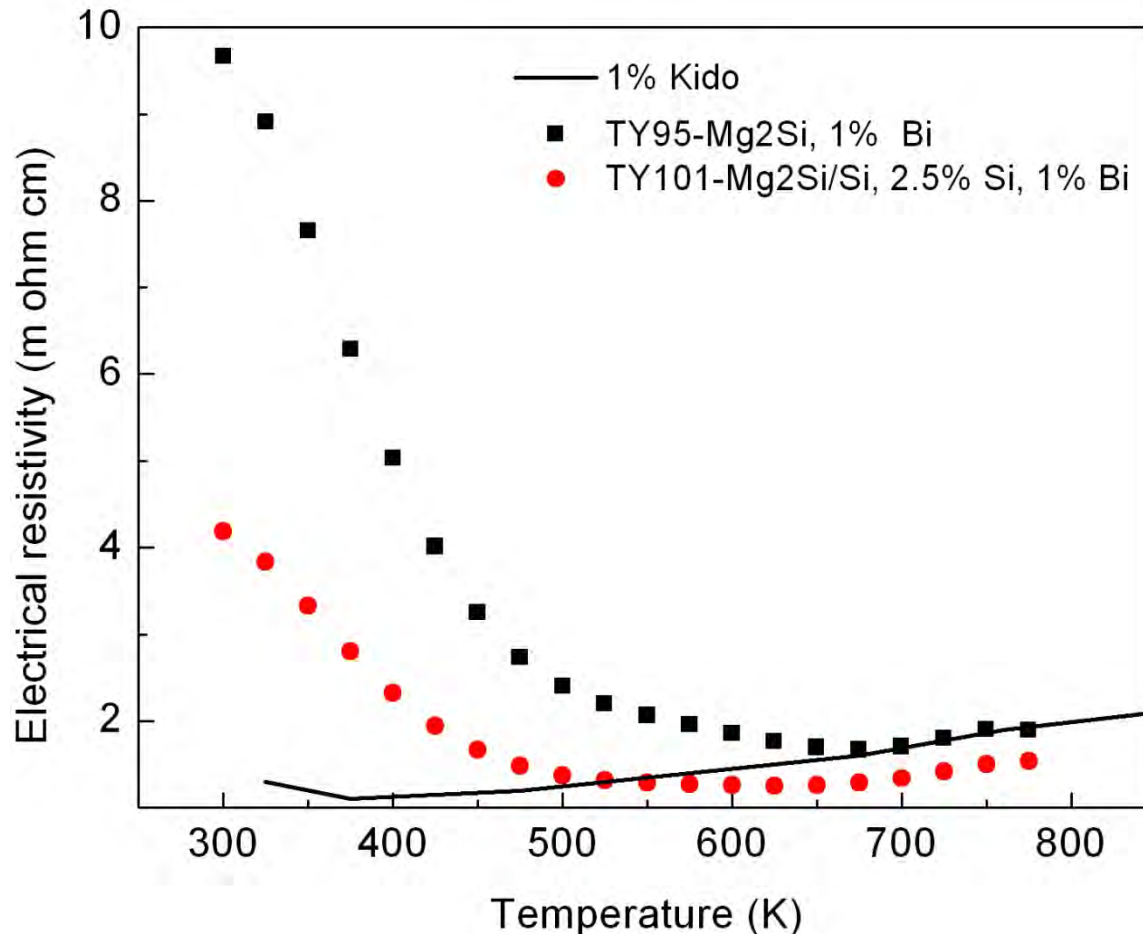
## Transport Properties: Mobility



We see impurity scattering at low temperatures. We are planning additional characterizations to see if we can understand this. It is possible that grain boundaries contributing to this effect.

# Progress

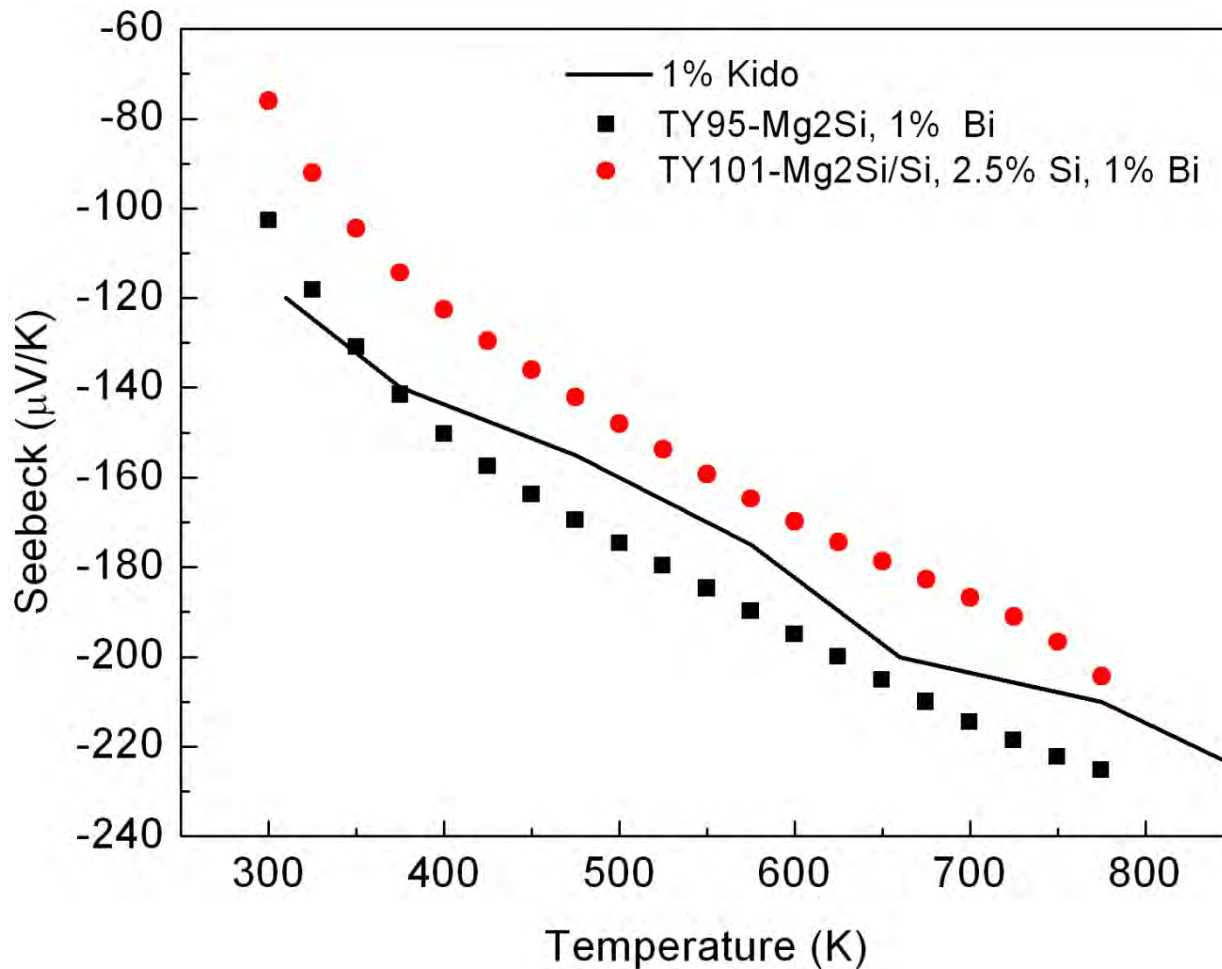
## Transport Properties: Electrical Resistivity



This shows the expected resistivity for doped Mg<sub>2</sub>Si, behaving like a normal heavily doped semiconductor. The two samples made by our method show impurity scattering at low temperatures.

# Progress

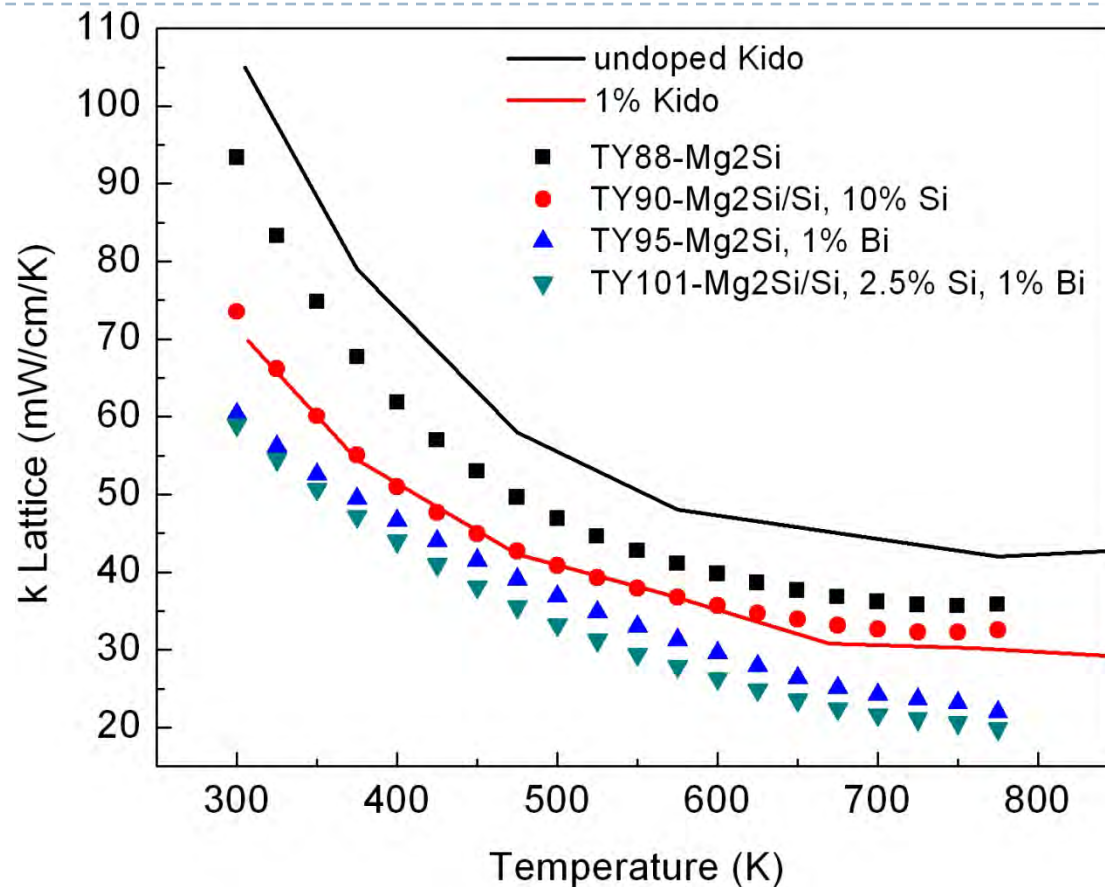
## Transport Properties: Seebeck



Seebeck is as expected for a degenerate semiconductor

# Progress:

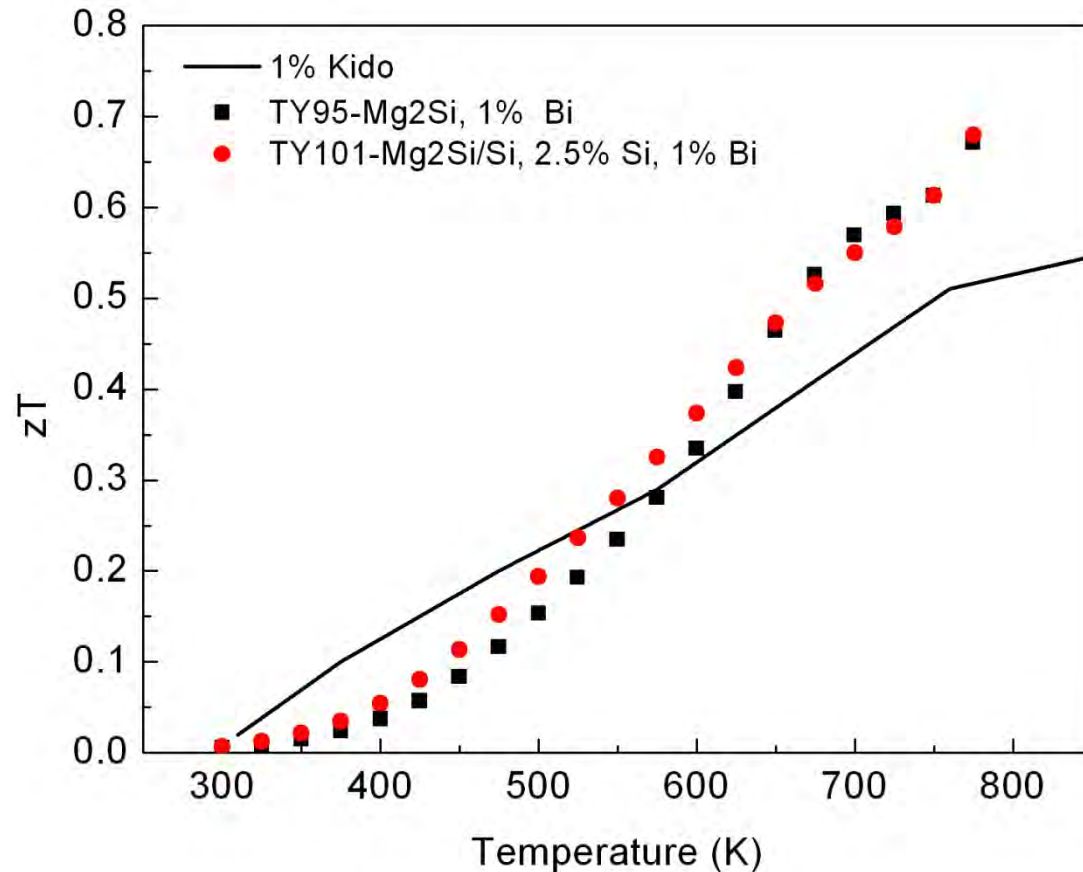
## Transport Properties: Thermal Conductivity



- ❑ Extracted lattice thermal conductivity: Measure thermal conductivity using laser flash method and subtracting the electronic contribution
- ❑ The results are comparable (and slightly lower) than that of Kido et al.

# Technical Accomplishments

## Transport Properties: Figure of Merit (ZT)



The figure of merit ZT of 1% Bi doped Mg<sub>2</sub>Si with 5% of Si nanocomposite is 0.68 at 775 K, which is approximately 30% improvement compared to 1% Bi doped Mg<sub>2</sub>Si (ZT ~0.52) reported by Tani, Kido, *Physica B* **2005**, 364 (1-4), 218-224.

# Collaborations

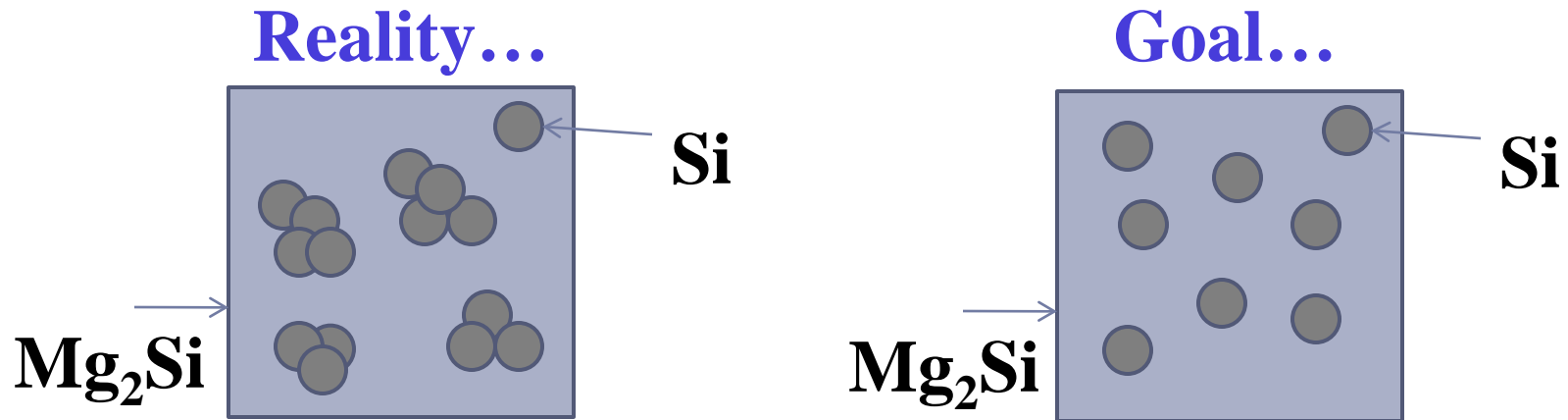
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  - ▶ **Sabah Bux, and Jean-Pierre Fleurial**  
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# Proposed Future Work

- ❑ Detailed comparison of theory/experiment; understand the origin of mobility degradation at low temperatures
- ❑ Optimize the growth condition (make the silicon nanoparticles isolated and homogeneously distributed with the assistance of solution synthesis)
- ❑ Identify high performance p-doping (Year 2)
- ❑ Improve ZT by optimizing nanoparticle size and potential distribution profile



# Summary

- ▶ Optimization of  $\text{Mg}_2\text{Si}$  Composites for thermoelectric waste heat recovery in vehicle exhaust has been investigated
- ▶ Technical Accomplishments
  - ▶ Preliminary electron transport modeling based on Boltzmann including two conduction bands and impurity/phonon scattering (Seebeck of bulk  $\text{Mg}_2\text{Si}$ )
  - ▶ Preliminary thermal conductivity modeling (optimum Si nanoparticle size for minimum lattice thermal conductivity)
  - ▶ A series of  $\text{Mg}_2\text{Si}$  samples with embedded Si nanoparticles have been synthesized and extensively characterized in a wide temperature range.
  - ▶ Current  $ZT \sim 0.7$  at 800K shows 30% improvement compared to bulk  $\text{Mg}_2\text{Si}$ .
  - ▶ Microprobe shows that Si rich areas are at micro level (agglomeration), and Bi is preferentially distributed in  $\text{Mg}_2\text{Si}$ .
  - ▶ We are investigating the cause of additional impurity scattering at low temperatures.